

## Interazione delle particelle pesanti cariche con la materia

Particelle pesanti cariche ->  $m \geq m(\text{protone})$

Perdita di energia specifica  
(calcolo quanto-relativistico di Bethe-Bloch)

$$\frac{dE}{dx} = 4\pi N Z \frac{z^2 e^4}{m_e c^2 \beta^2} \left[ \ln \frac{2m_e c^2 \gamma^2 \beta^2}{I} - \beta^2 \right]$$

con

$$I = 12 Z \text{ eV}$$

energia media di ionizzazione

$N$  la densità numerica degli atomi del materiale

$Z$  il numero di elettroni per atomo

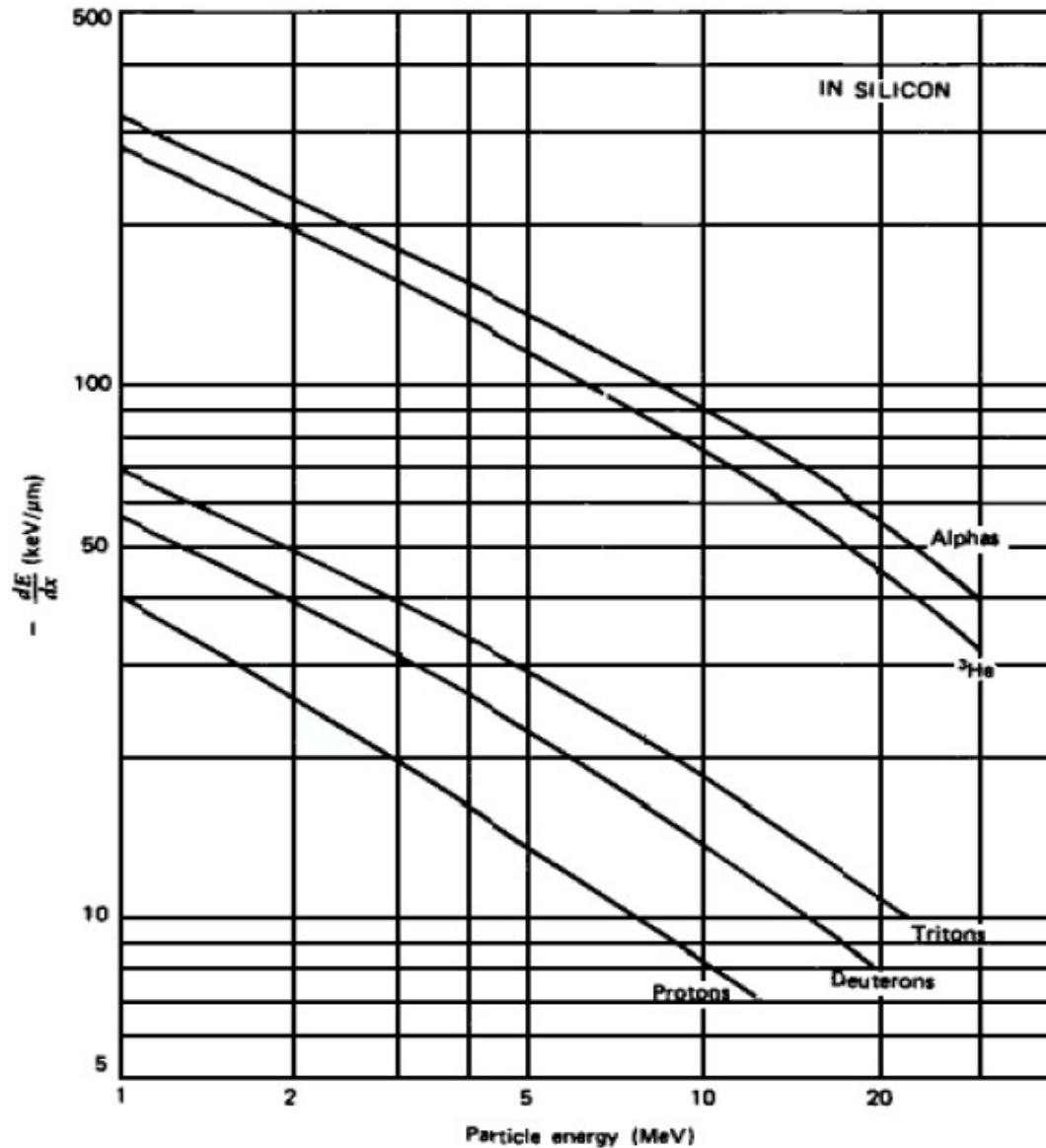
$ze$  la carica dello ione proiettile

**Interazione delle particelle pesanti cariche con la materia**

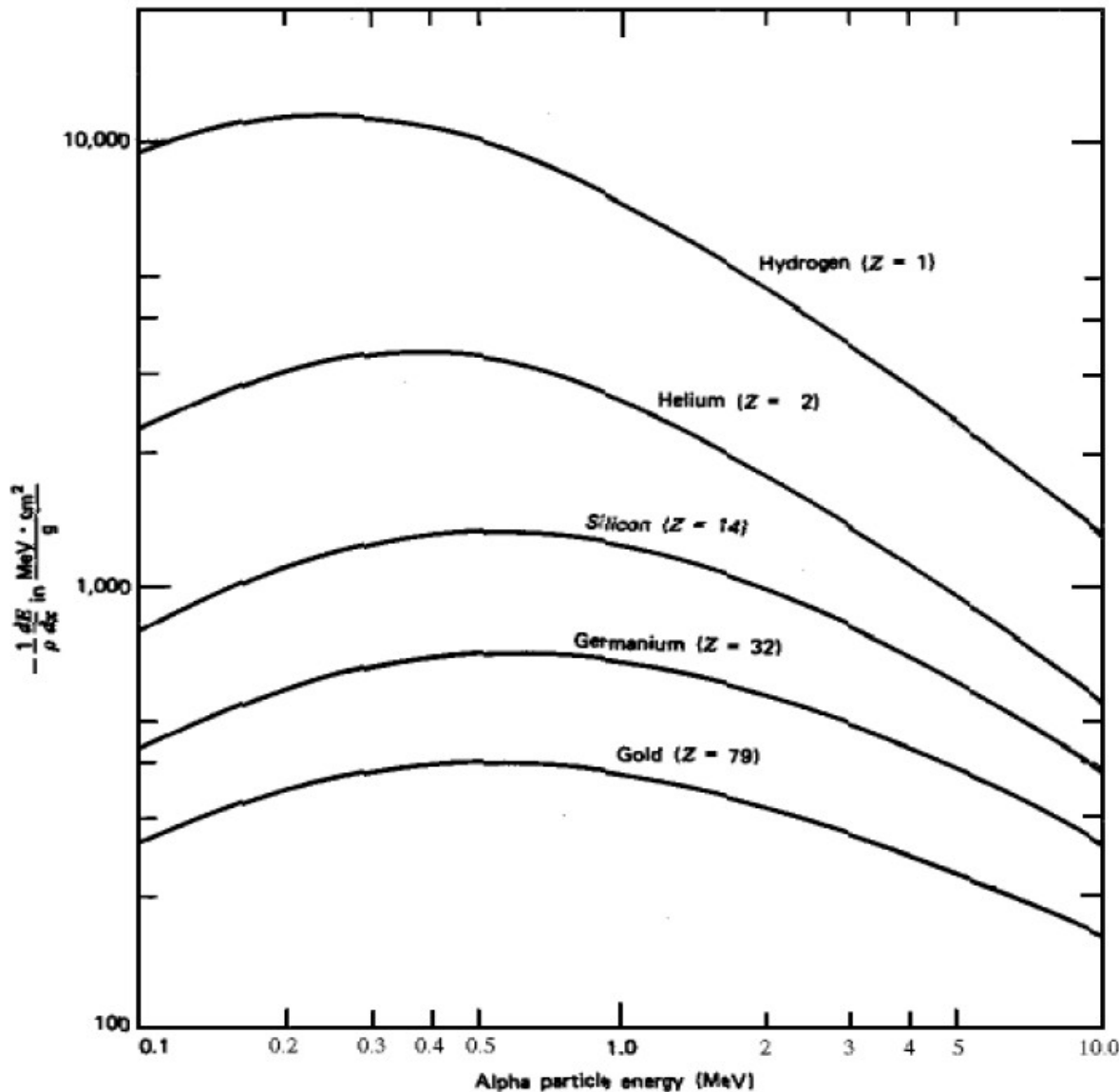
$$\frac{dE}{dx} = 4\pi N Z \frac{z^2 e^4}{m_e c^2 \beta^2} \left[ \ln \frac{2m_e c^2 \gamma^2 \beta^2}{I} - \beta^2 \right]$$

**Dipendenza da caratteristiche del proiettile**

**A parità di energia:**  
- dipendenza da  $m$   
- dipendenza da  $z^2$



**Figure 2-9** The specific energy loss calculated for different charged particles in silicon. (From Skyrme.<sup>3</sup>)



**Figure 2-10** The specific energy loss calculated for alpha particles in different materials. Values are normalized by the density of the absorber material. (Data from Williamson et al.<sup>4</sup>)

Interazione delle particelle pesanti cariche con la materia

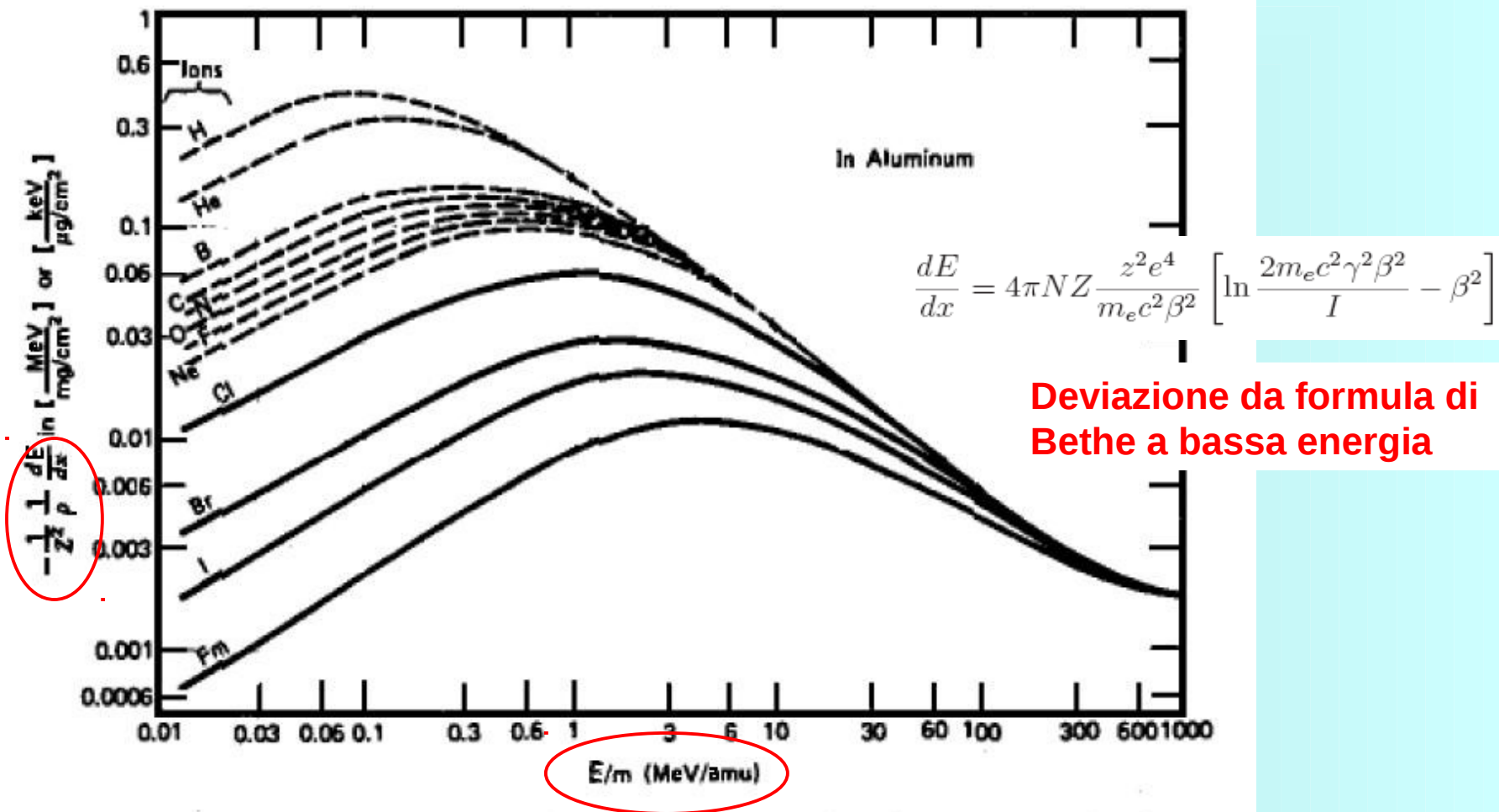
$$\frac{dE}{dx} = 4\pi NZ \frac{z^2 e^4}{m_e c^2 \beta^2} \left[ \ln \frac{2m_e c^2 \gamma^2 \beta^2}{I} - \beta^2 \right]$$

Dipendenza da caratteristiche del bersaglio

$dE/dx \propto NZ = N_{Av} \rho Z / A$  e quindi  
 $(1/\rho)(dE/dx) \propto Z / A$

Residua dipendenza di  $(1/\rho)(dE/dx)$  da  $Z$  da cui dipende anche  $I$

## Interazione delle particelle pesanti cariche con la materia



**Figure 2-11** Plots showing the specific energy loss of various heavy ions in aluminum. The abscissa is the ion energy divided by its mass, and the ordinate is  $-dE/dx$  divided by the density of aluminum and the square of the ion atomic number. Typical fission fragments (e.g., iodine) show a continuously decreasing  $-dE/dx$  while slowing from their initial energy ( $\sim 1$  MeV/amu). (From Northcliffe and Schilling.<sup>7</sup>)

## Interazione delle particelle pesanti cariche con la materia

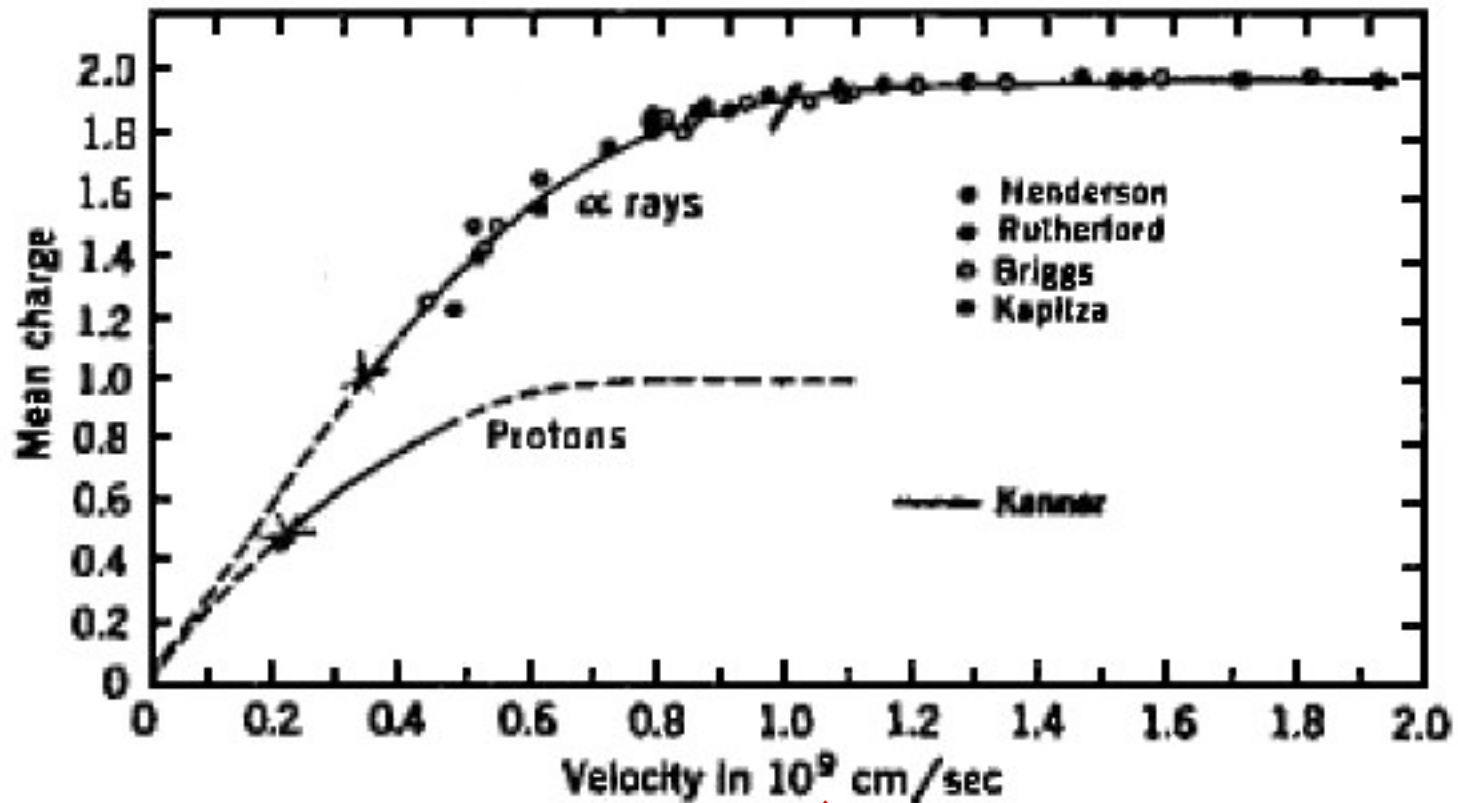
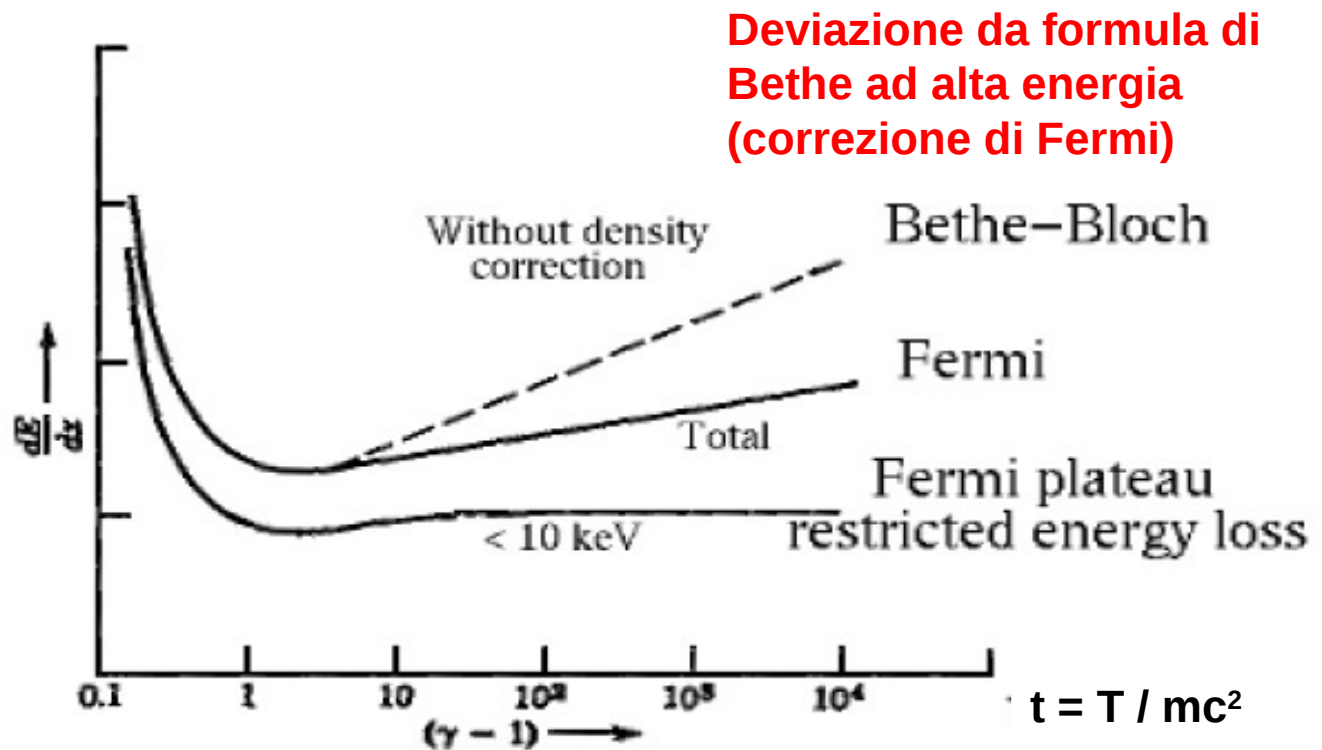


Fig. 1.1 Mean charge  $z_{av}$  for  $\alpha$  rays and protons, due to capture and loss of electrons.

$$v (10^9 \text{ cm/s}) = 1.39 * \text{sqrt} (E(\text{MeV}) / A)$$

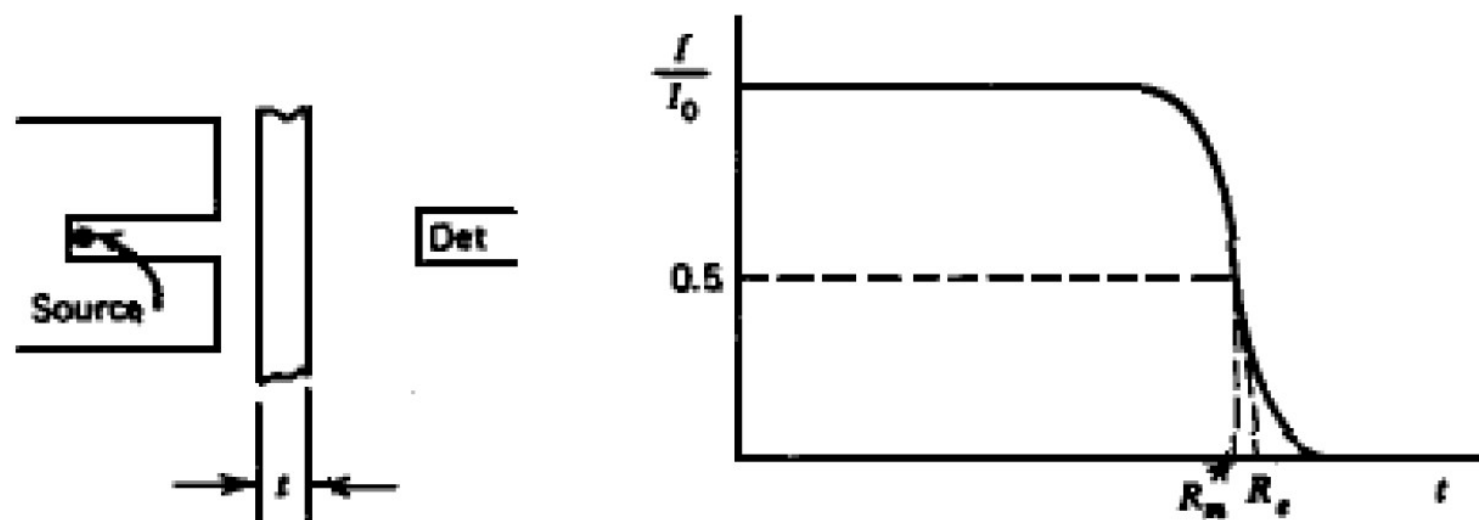
## Interazione delle particelle pesanti cariche con la materia



**Fig. 13.5** Energy loss, including the density effect. The dotted curve is the total energy loss without density correction. The solid curves have the density effect incorporated, the upper one being the total energy loss and the lower one the energy loss due to individual energy transfers of less than 10 keV.

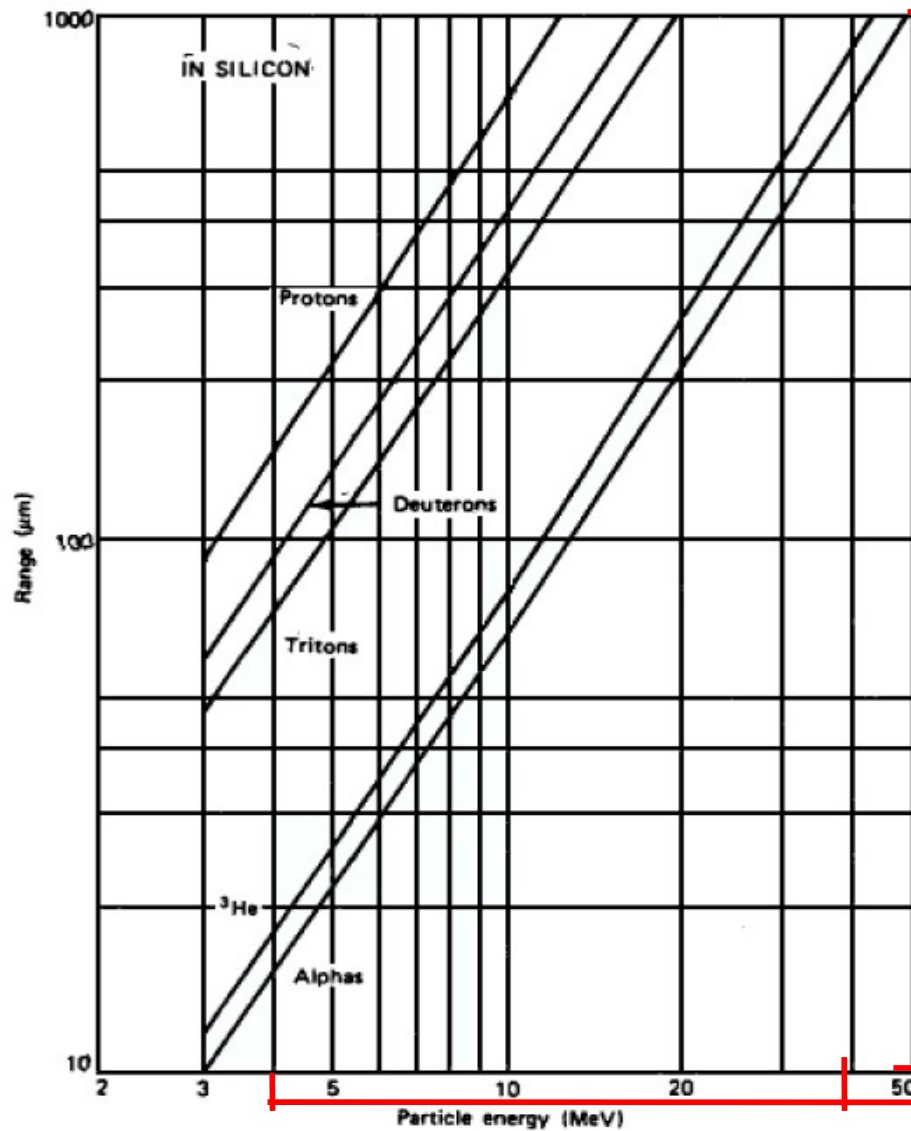
## Interazione delle particelle pesanti cariche con la materia

### RANGE



**Figure 2-5** An alpha particle *transmission* experiment.  $I$  is the detected number of alpha particles through an absorber thickness,  $t$ , whereas  $I_0$  is the number detected without the absorber. The mean range  $R_m$  and extrapolated range  $R_e$  are indicated.





**Figure 2-7** Range-energy curves calculated for different charged particles in silicon. The near-linear behavior of the log-log plot over the energy range shown suggests an empirical relation of the form  $R = aE^b$ , where the slope-related parameter  $b$  is not greatly different for the various particles. (From Skyrme.<sup>3</sup>)

Interazione delle particelle pesanti cariche con la materia

## RANGE

Indicando con  $u$  la velocità del proiettile la formula di Bethe può essere riscritta come

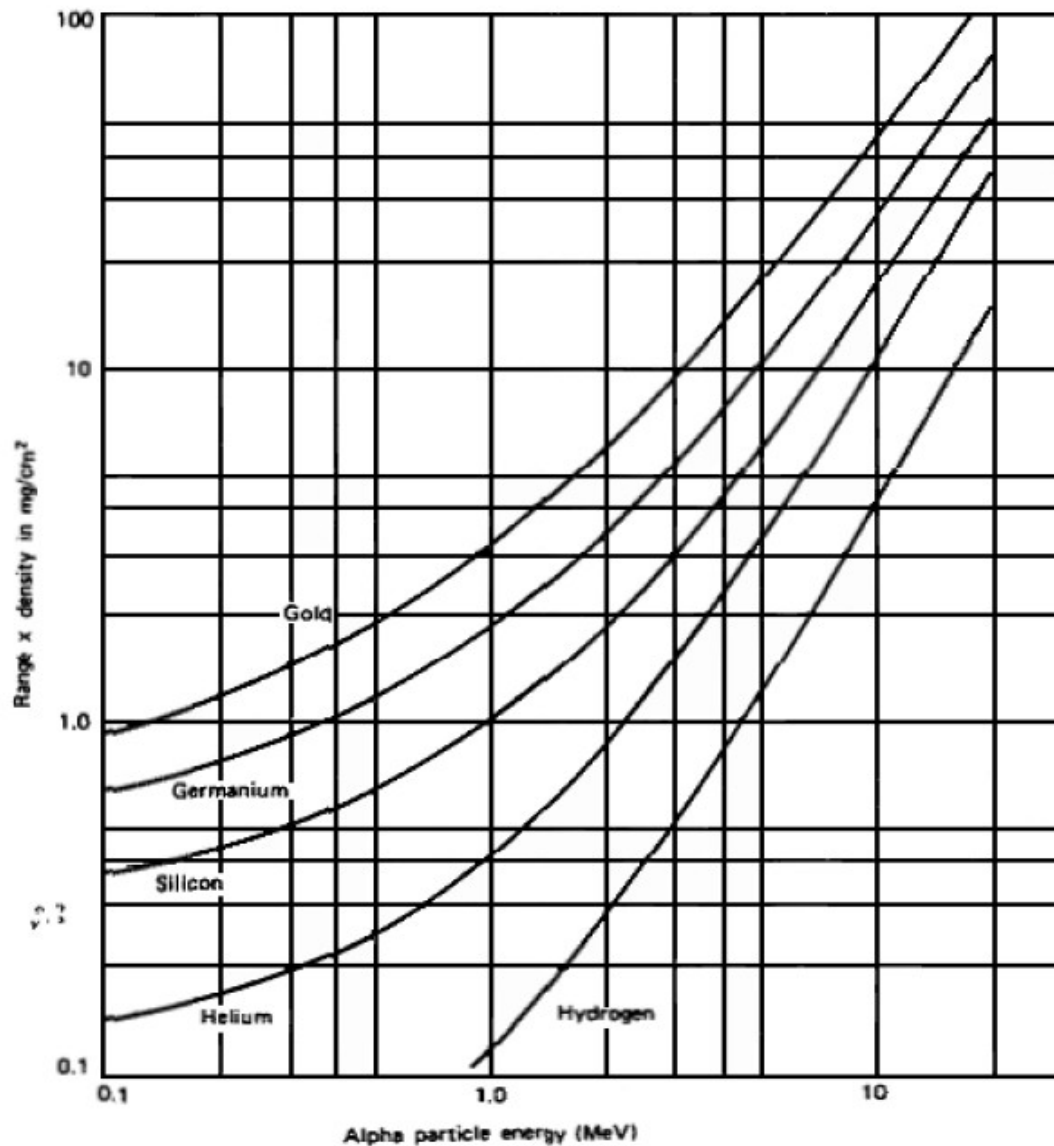
$$dx = \frac{m_1}{z_1^2} \frac{m_e}{4\pi e^4} \frac{1}{NZ} \frac{u^3 du}{\ln(2m_e u^2/I)}$$

$$R = \frac{m_1}{z_1^2} \int_{u_i}^0 f(u) du$$

$$R \approx k m_1 u^4 / z_1^2 = k' E^2 / m_1 z_1^2$$

Fattore 100  
Fattore 10





**Figure 2-8** Range-energy curves calculated for alpha particles in different materials. Units of the range are given in mass thickness (see Section III.B.2) to minimize the differences in these curves. (Data from Williamson et al.<sup>4</sup>)

Interazione delle particelle pesanti cariche con la materia

## RANGE

$$dx = \frac{m_1}{z_1^2} \frac{m_e}{4\pi e^4} \frac{1}{NZ} \frac{u^3 du}{\ln(2m_e u^2/I)}$$

$$R \approx k' m_1 u^4 / NZ z_1^2$$

Per particelle alfa incidenti:

dipendenza da Z di  $R \cdot \rho = R \cdot NM_m / N_A$   
con  $M_m$  massa molare

# Interazione degli elettroni con la materia

## Perdita di energia specifica collisionale

Particelle cariche pesanti

$$\frac{dE}{dx} = 4\pi N Z \frac{z^2 e^4}{m_e c^2 \beta^2} \left[ \ln \frac{2m_e c^2 \gamma^2 \beta^2}{I} - \beta^2 \right]$$

Elettroni

$$\left( \frac{dE}{dx} \right)_{coll} = 4\pi \frac{N Z e^4}{m_e \beta^2 c^2} \cdot \left\{ \ln \frac{(\gamma - 1)(\gamma + 1)^{1/2}}{2^{1/2}} \frac{m_e c^2}{I} - \beta^2 \right. \\ \left. + [1 - \ln 2(2(1 - \beta^2)^{1/2} - 1 + \beta^2) + \frac{1}{8}(1 - (1 - \beta^2)^{1/2})^2] \right\}$$

Termine correttivo del 10-20%

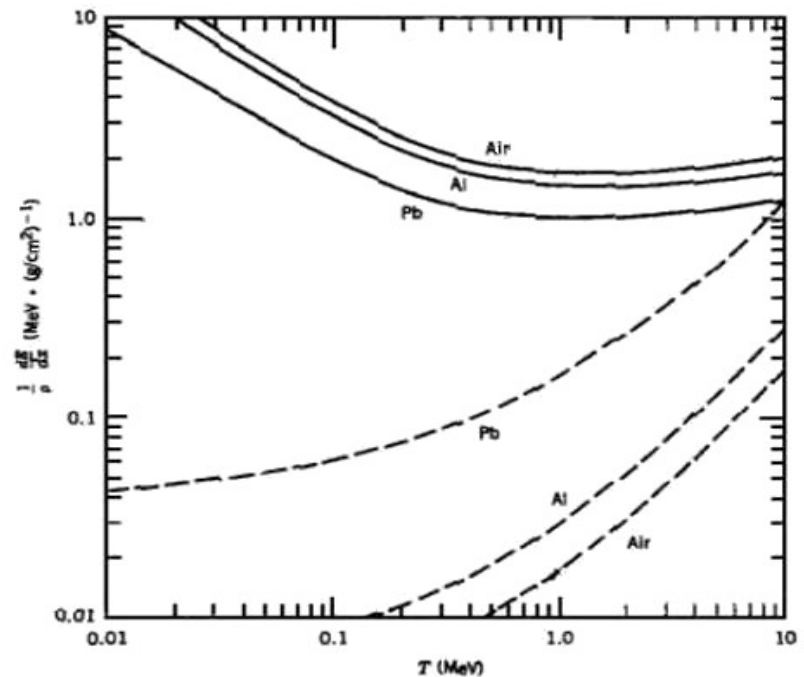
## Interazione degli elettroni con la materia

### Perdita di energia specifica radiativa

$$\left(\frac{dE}{dx}\right)_{rad} = -(4/137)Z^2e^4N_0\frac{T_e + m_e c^2}{(m_e c^2)^2} \left[ \ln \frac{2(T_e + m_e c^2)}{m_e c^2} - \frac{1}{3} \right]$$

$$\frac{(dE/dx)_r}{dE/dx)_c} \sim \frac{(t + 1) Z}{1600}$$

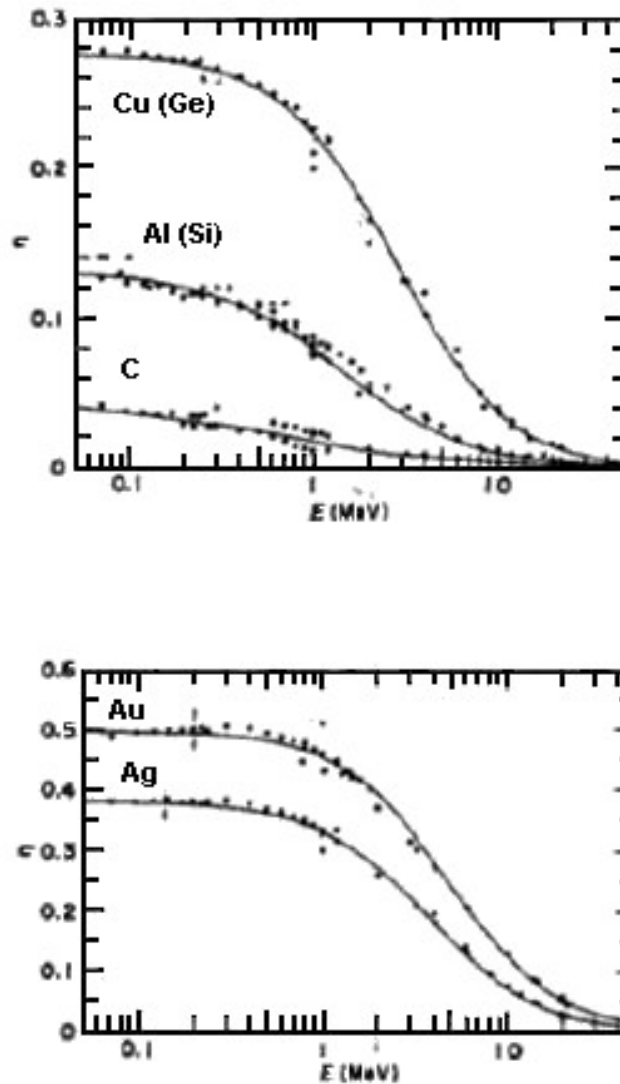
$$t = T_e / m_e c^2$$



**Figure 7.3** Energy loss by electrons in air, Al, and Pb. To suppress the large variation in  $dE/dx$  arising from the number of electrons of the material, the quantity  $\rho^{-1}(dE/dx)$  is plotted. Solid lines are for collisions; dashed lines are for radiation. For additional tabulated data on energy losses, see L. Pages et al., *Atomic Data* 4, 1 (1972).

## Interazione degli elettroni con la materia

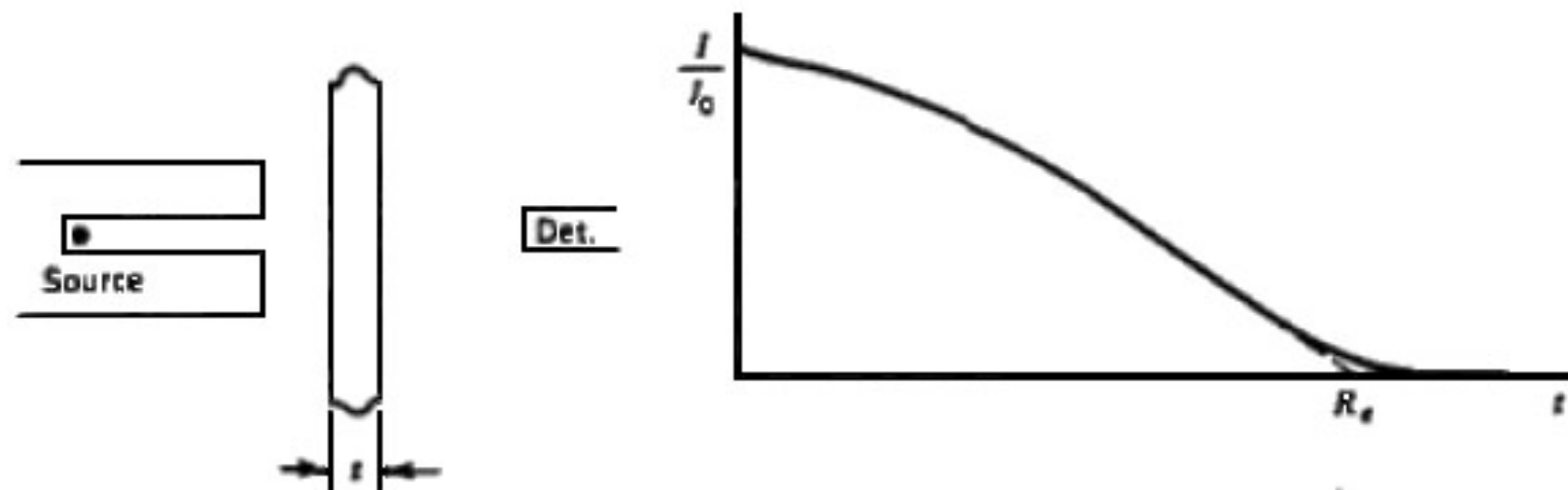
### Back-scattering



**Figure 2-17** Fraction  $\eta$  of normally incident electrons that are backscattered from thick slabs of various materials, as a function of incident energy  $E$ . (From Tabata et al.<sup>18</sup>)

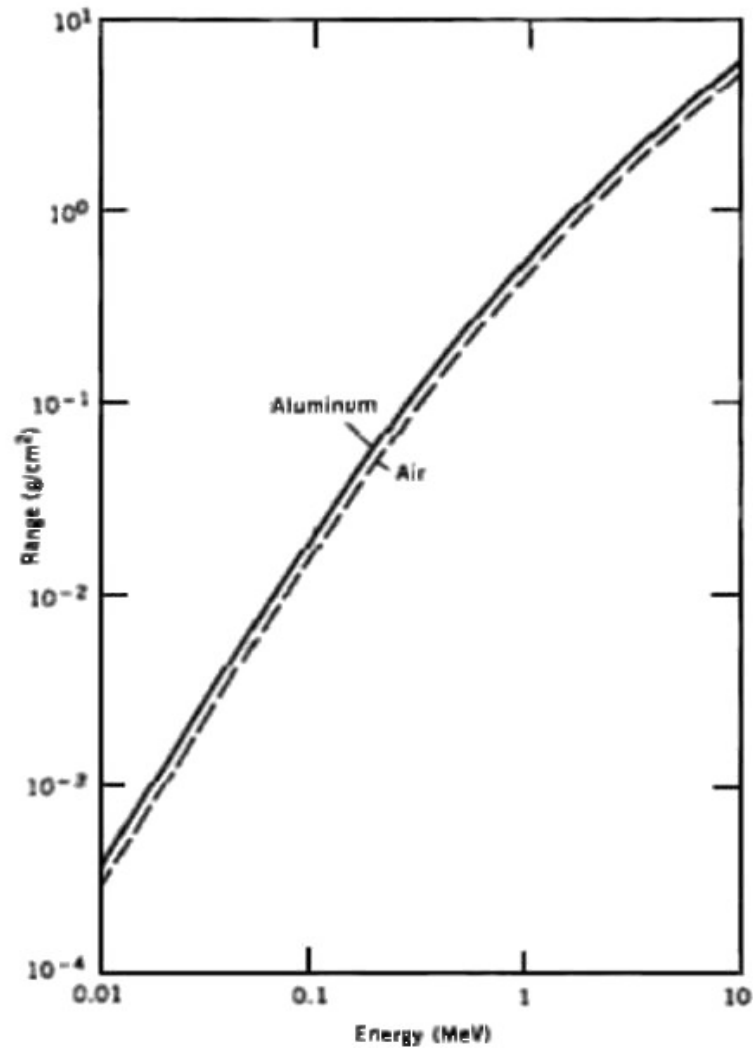
## Interazione degli elettroni con la materia

### RANGE



**Figure 2-13** Transmission curve for monoenergetic electrons.  $R_e$  is the extrapolated range.

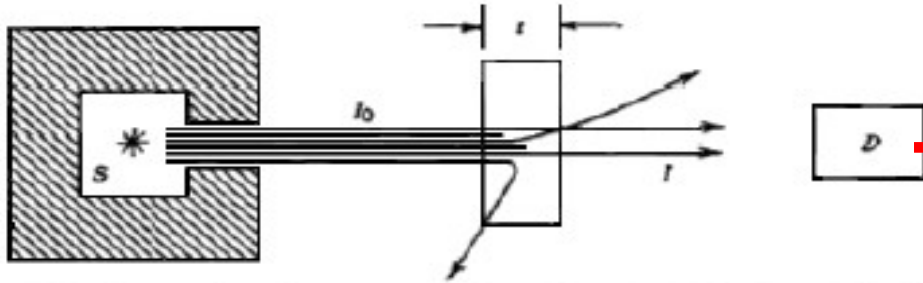
## Interazione degli elettroni con la materia



**Figure 7.4** Range-energy relationship for electrons in air and in aluminum.

RANGE

## Interazione della radiazione e.m. con la materia



**Figure 7.9** An experiment to measure absorption of radiation in a slab of material of thickness  $t$ . A beam of radiation from the source S is collimated and then is scattered or absorbed by the material. The remaining intensity  $I$  reaches the detector D.

$$dn_c = (NZ dx)\sigma_c n$$

coefficiente di  
attenuazione lineare

$$\sigma = N Z \sigma_c \text{ cm}^{-1}$$

$$n = n_0 e^{-\sigma x} = n_0 e^{-\frac{\sigma}{\rho}(\rho x)}$$

$$\frac{\sigma}{\rho} = N_A \frac{Z}{M_m} \sigma_c \text{ g}^{-1} \text{ cm}^2$$

coefficiente di  
attenuazione lineare di massa



# Interazione della radiazione e.m. con la materia

## Principali interazioni

### •Effetto fotoelettrico

per  $E_\gamma > BE_K$

$$\sigma_{ph}(\text{per 1 elettrone 1s}) = \frac{128\pi}{3} \frac{e^2 h}{m_e c E_\gamma} \left(\frac{BE_K}{E_\gamma}\right)^3 \frac{e^{-4\varepsilon \arctan(1/\varepsilon)}}{1 - e^{-2\pi\varepsilon}} \text{ cm}^2$$

$$\varepsilon = [BE_K / (E_\gamma - BE_K)]^{1/2}$$

per  $E_\gamma \approx BE_K$

$$\sigma_{ph}(\text{per 1 elettrone 1s}) \approx \frac{6.31 \cdot 10^{-18}}{Z^2} \left(\frac{BE_K}{E_\gamma}\right)^{8/3} \text{ cm}^2$$

### •Scattering Compton

$$\sigma_c = 2\pi r_e^2 \left\{ \frac{1 + \alpha}{\alpha^2} \left[ \frac{2(1 + \alpha)}{1 + 2\alpha} - \frac{1}{\alpha} \ln(1 + 2\alpha) \right] + \frac{1}{2\alpha} \ln(1 + 2\alpha) - \frac{(1 + 3\alpha)}{(1 + 2\alpha)^2} \right\} \frac{\text{cm}^2}{\text{elettrone}}$$

$$\alpha = h\nu / m_e c^2$$

### •Creazione di coppie

Per  $h\nu \gg m_e c^2$

$$\sigma_{pair} = \frac{Z^2}{137} r_e^2 \left( \frac{28}{9} \ln 183 Z^{-1/3} - \frac{2}{27} \right) \text{ cm}^2$$

$E_\gamma$



## Interazione della radiazione e.m. con la materia

### •Effetto fotoelettrico

$$\sigma_{ph}(\text{per 1 elettrone 1s}) \simeq \frac{6.31 \cdot 10^{-18}}{Z^2} \left( \frac{BE_K}{E_\gamma} \right)^{8/3} \text{ cm}^2$$

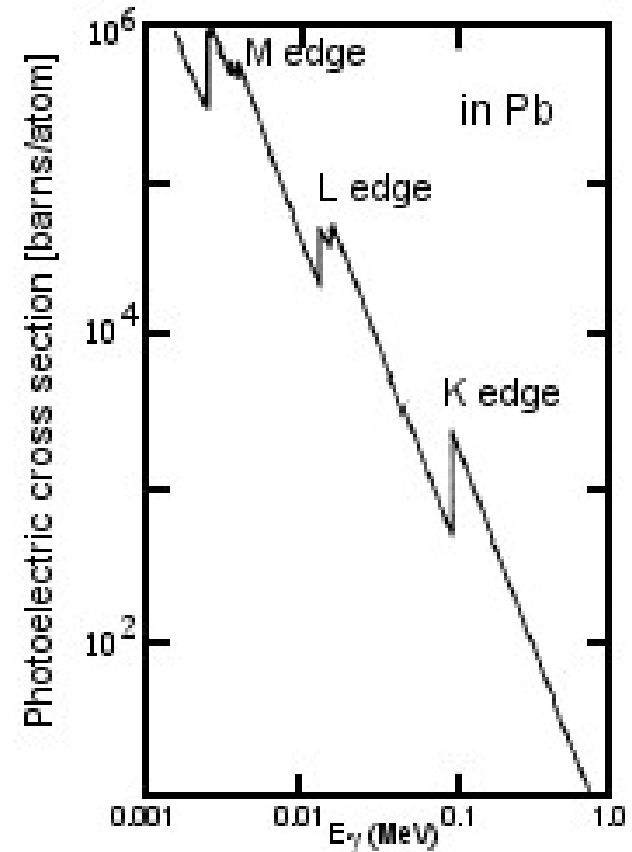
$$BE_K \sim 13.5(Z-1)^2 \text{ eV}$$

$$BE_L \sim 13.5(Z-5)^2/4 \text{ eV}$$

$$BE_M \sim 13.5(Z-13)^2/9 \text{ eV}$$

coefficiente di attenuazione lineare per effetto fotoelettrico

$$\tau = \left\{ (5 \div 6) / 4 \right\} \sigma_{ph} N \text{ cm}^{-1}$$



**Figure 7.5** Photoelectric cross section in Pb. The discrete jumps correspond to the binding energies of various electron shells; the K-electron binding energy, for example, is 88 keV. To convert the cross section to the linear absorption coefficient  $\tau$  in  $\text{cm}^{-1}$ , multiply by 0.033.

## Interazione della radiazione e.m. con la materia

### Effetto fotoelettrico

### Distribuzione angolare dei fotoelettroni

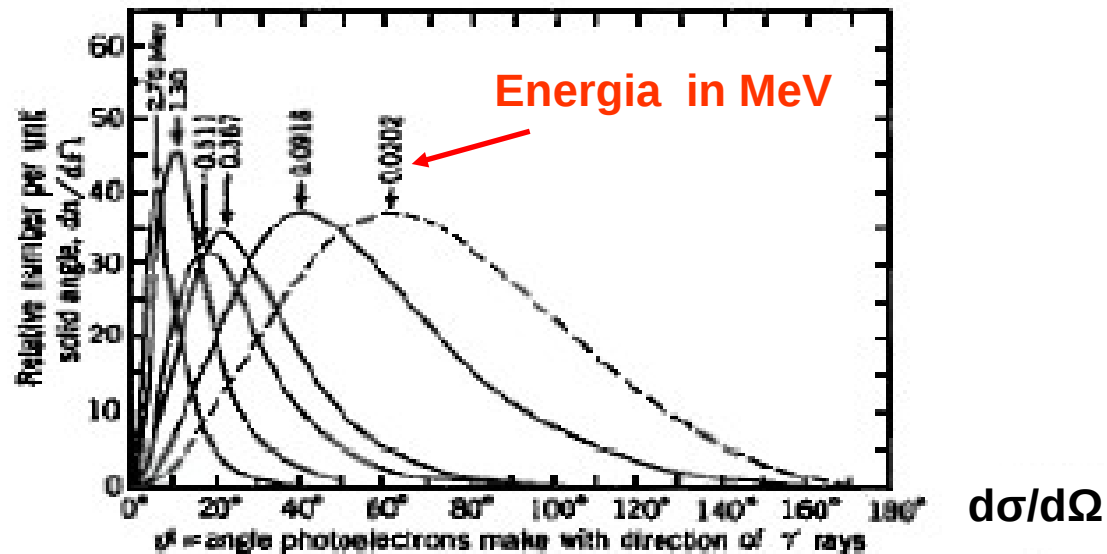


Fig. 1.2 Directional distribution of photoelectrons per unit solid angle, for energies as marked. The curves are not normalized with respect to each other. Solid curves are calculated from Sauter's (S5) relativistic formula; dashed curve from Fischer's (F50) nonrelativistic formula. [From Davison and Seane (D12).]

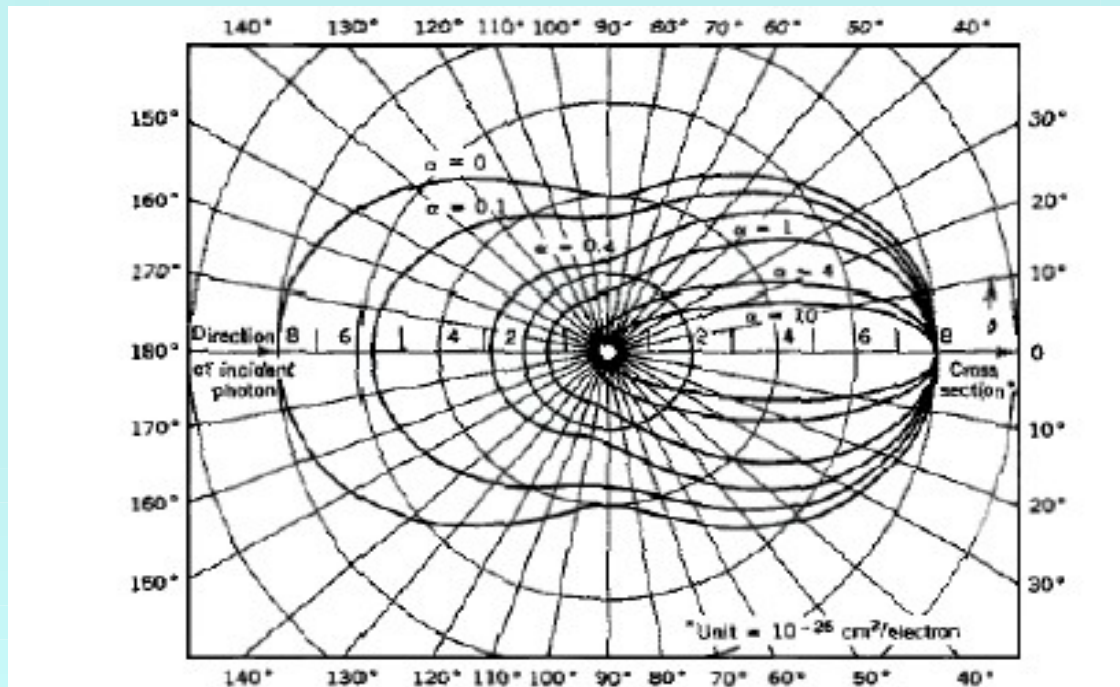
## Interazione della radiazione e.m. con la materia

### Scattering Compton

$$\frac{d\sigma_c}{d\Omega} = \frac{r_e^2}{2} \left( \frac{\nu^*}{\nu} \right)^2 \left( \frac{\nu}{\nu^*} + \frac{\nu^*}{\nu} - \sin^2 \theta \right)$$

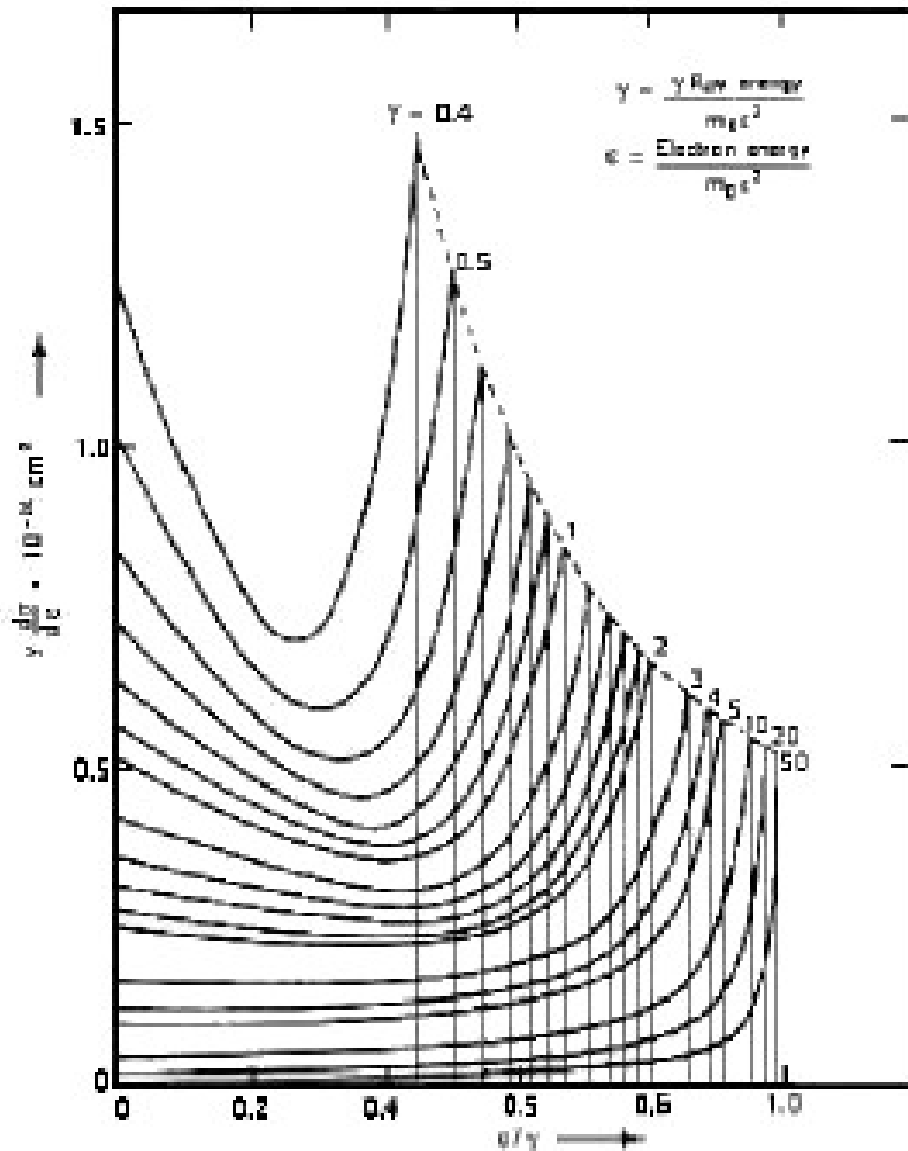
con

$$\frac{h\nu^*}{h\nu} = \frac{\nu^*}{\nu} = \frac{1}{1 + \alpha(1 - \cos \theta)}$$



**Figure 7.7** The Compton-scattering cross section for various incident energies. The polar plot shows the intensity of the scattered radiation as a function of the scattering angle  $\theta$ . From R. D. Evans, *The Atomic Nucleus* (New York: McGraw-Hill, 1955).

## Interazione della radiazione e.m. con la materia



### Scattering Compton

Energia dell'elettrone di rinculo

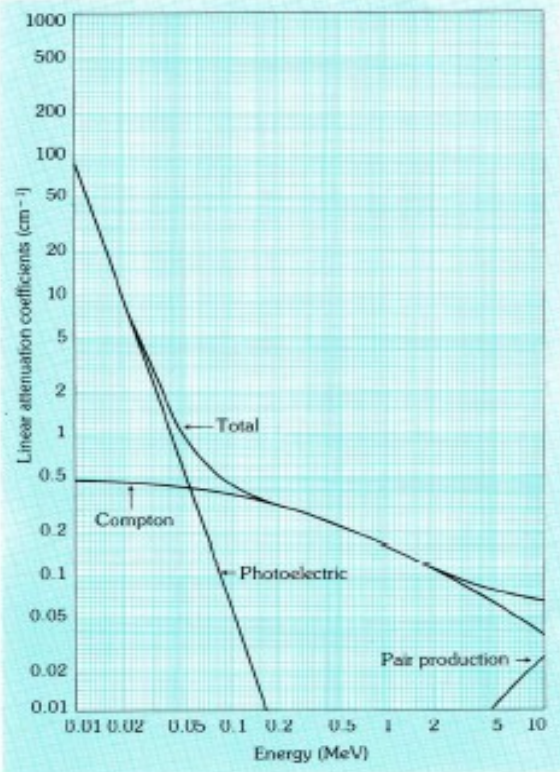
$$t_e = \frac{\alpha^2(1 - \cos \theta)}{1 + \alpha(1 - \cos \theta)}$$

Distribuzione in energia dei fotoelettroni

$$\left(\frac{d\sigma}{dt_e}\right) \frac{1}{\pi r_e^2} = \frac{2\alpha^4 - 2\alpha^2(2\alpha + 1)t_e + (3\alpha^2 + 2\alpha + 1)t_e^2 - \alpha t_e^3}{\alpha^4(\alpha - t_e)^2}$$

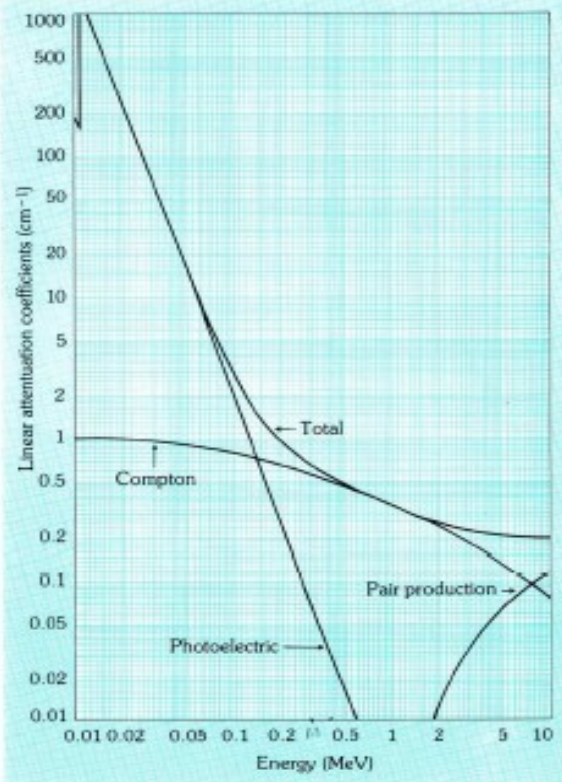
## Interazione della radiazione e.m. con la materia

Si



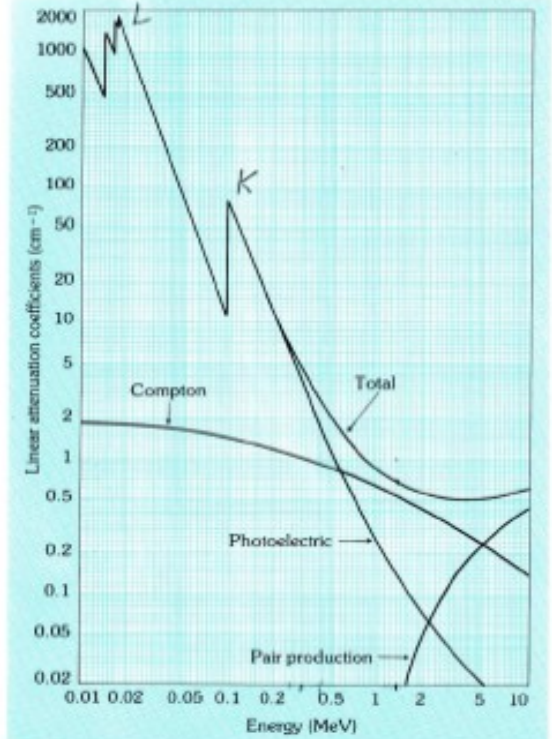
Specific mass = 2420  $\text{kg}/\text{m}^3$   
 Atomic number:  $Z = 14$   
 Electron Binding Energy:  
 K-edge = 1.84 keV  
 Average K X-Ray Energy: 1.75 keV

Ge



Specific mass = 5350  $\text{kg}/\text{m}^3$   
 Atomic number:  $Z = 32$   
 Electron Binding Energy:  
 K-edge = 11.1 keV  
 Average K X-Ray Energy = 10 keV

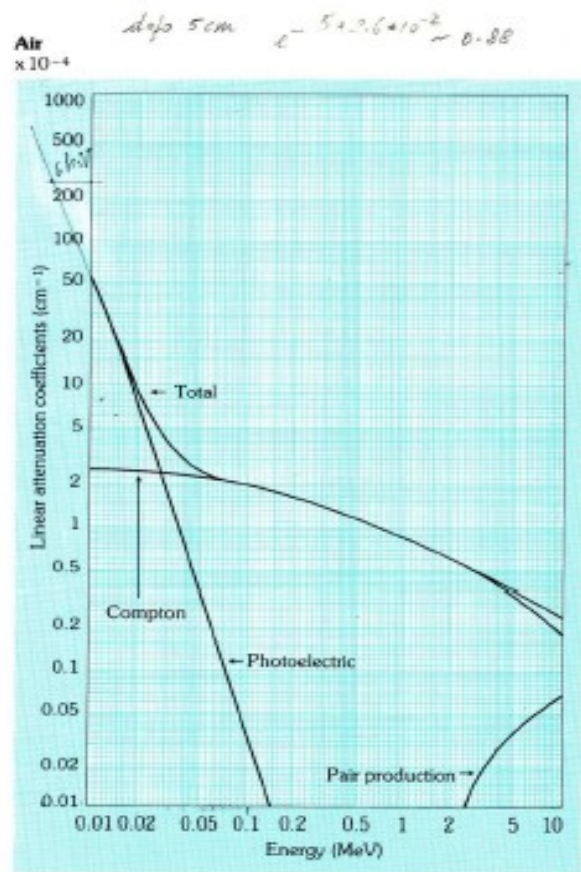
Pb



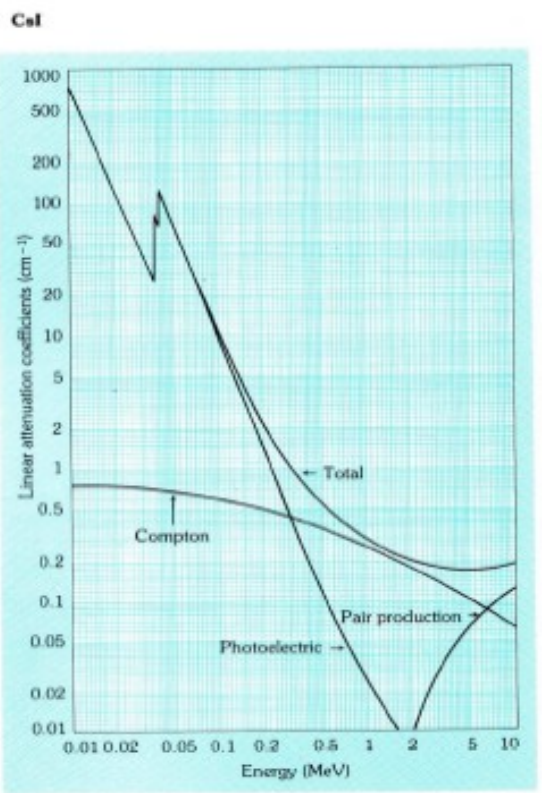
Specific mass = 11350  $\text{kg}/\text{m}^3$   
 Atomic number:  $Z = 82$   
 Electron Binding Energies:  
 K-edge = 88.02 keV  
 L<sub>1</sub>-edge = 15.87 keV  
 L<sub>11</sub>-edge = 15.21 keV  
 L<sub>111</sub>-edge = 13.05 keV  
 Average K X-Ray Energy = 76.74 keV



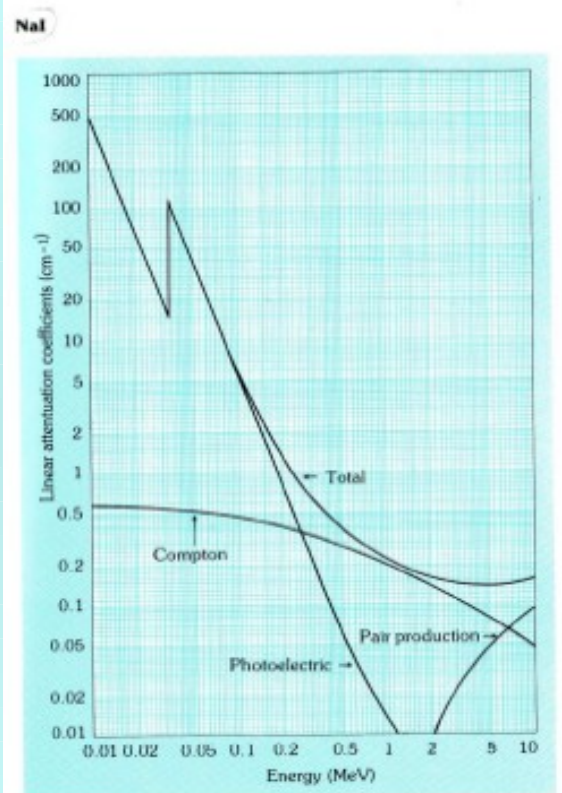
# Interazione della radiazione e.m. con la materia



Specific mass = 1.293 kg/m<sup>3</sup>  
 Composition of "air"  
 78.04 volume percent nitrogen  
 21.02 volume percent oxygen  
 0.94 volume percent argon



Specific mass = 4510 kg/m<sup>3</sup>  
 Atomic number: Z (I) = 53  
 Z (Cs) = 55  
 Electron Binding Energies:  
 K-edge (I) = 33.17 keV  
 K-edge (Cs) = 35.98 keV  
 L<sub>1</sub>-edge (Cs) = 5.72 keV  
 L<sub>11</sub>-edge (Cs) = 5.36 keV  
 L<sub>111</sub>-edge (Cs) = 5.01 keV  
 Average K X-Ray Energy (Cs) = 31.6

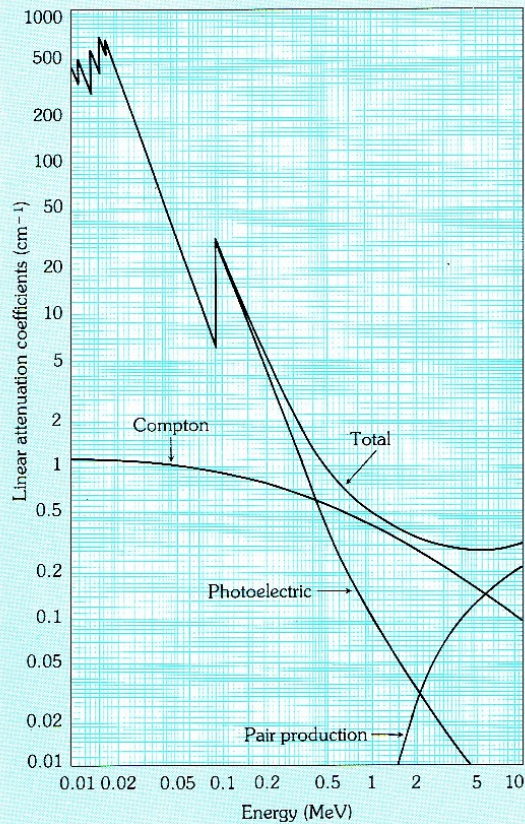


Specific mass = 3670 kg/m<sup>3</sup>  
 Atomic Number: Z (I) = 53  
 Z (Na) = 11  
 Electron Binding Energies:  
 K-edge (I) = 33.17 keV  
 L<sub>1</sub>-edge (I) = 5.19 keV  
 L<sub>11</sub>-edge (I) = 4.85 keV  
 L<sub>111</sub>-edge (I) = 4.56 keV  
 Average K X-Ray Energy (I) = 29.2 keV



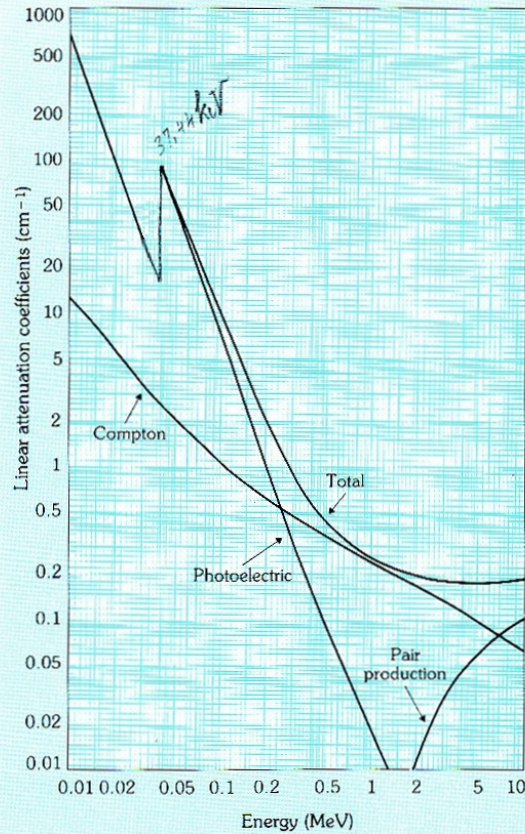
# Interazione della radiazione e.m. con la materia

**BGO**



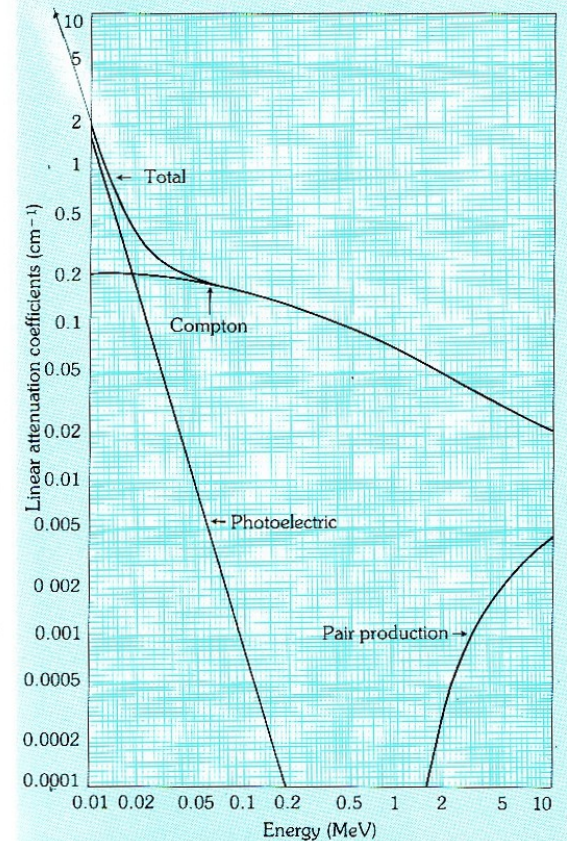
Specific mass = 7130 kg/m<sup>3</sup>  
 Atomic number: Z (Bi) = 83  
 Z (Ge) = 32  
 Electron Binding Energies:  
 K-edge (Bi) = 90.53 keV  
 L<sub>1</sub>-edge (Bi) = 16.39 keV  
 L<sub>11</sub>-edge (Bi) = 15.71 keV  
 L<sub>111</sub>-edge (Bi) = 13.42 keV  
 K-edge (Ge) = 11.10 keV  
 Average K X-Ray Energy (Bi) = 78.9 keV

**BaF<sub>2</sub>**



Specific mass = 4880 kg/m<sup>3</sup>  
 Atomic number: Z(Ba) = 56  
 Z(F) = 9  
 Electron Binding Energies:  
 K-edge (Ba) = 37.44 keV  
 L<sub>1</sub>-edge (Ba) = 5.99 keV  
 L<sub>11</sub>-edge (Ba) = 5.62 keV  
 L<sub>111</sub>-edge (Ba) = 5.25 keV  
 K-edge (F) = 0.69 keV

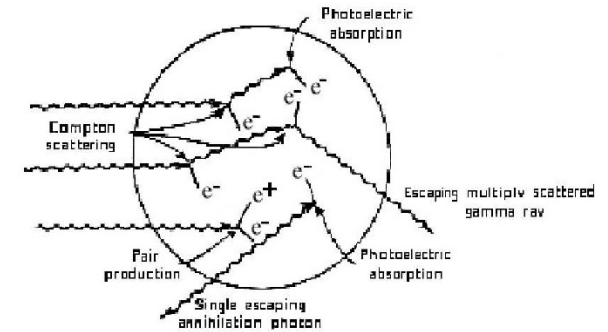
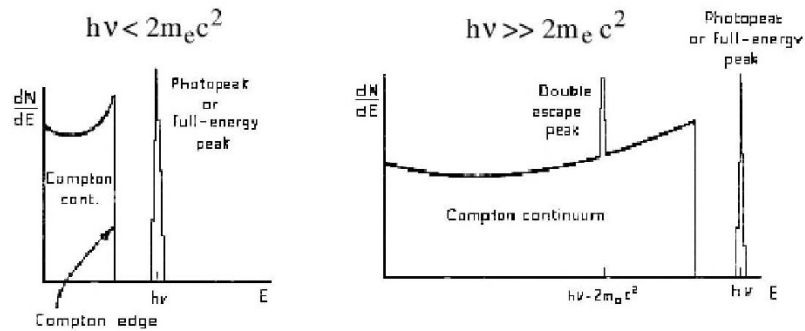
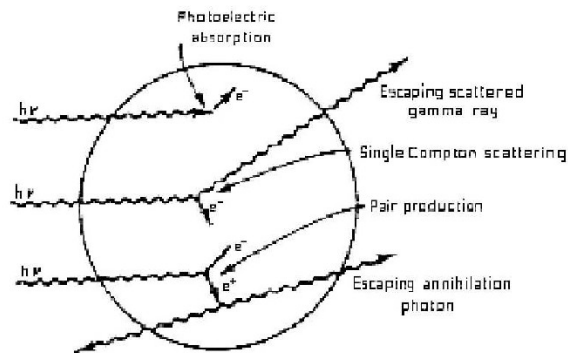
**Plastic Scintillator**



Specific mass = 1050 kg/m<sup>3</sup>  
 No atoms per cm<sup>3</sup>  
 H:  $5.25 \times 10^{22}$ , C:  $4.75 \times 10^{22}$   
 N:  $1.8 \times 10^{18}$ , O:  $1.8 \times 10^{18}$   
 Atomic number: Z (C) = 6  
 K-edge (C) = 0.28 keV

# Interazione della radiazione e.m. con la materia

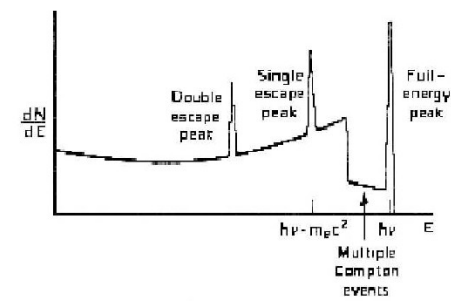
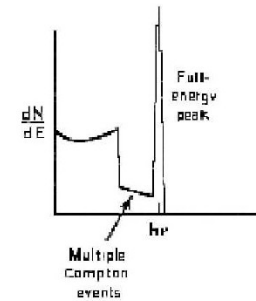
## “rivelatore piccolo”



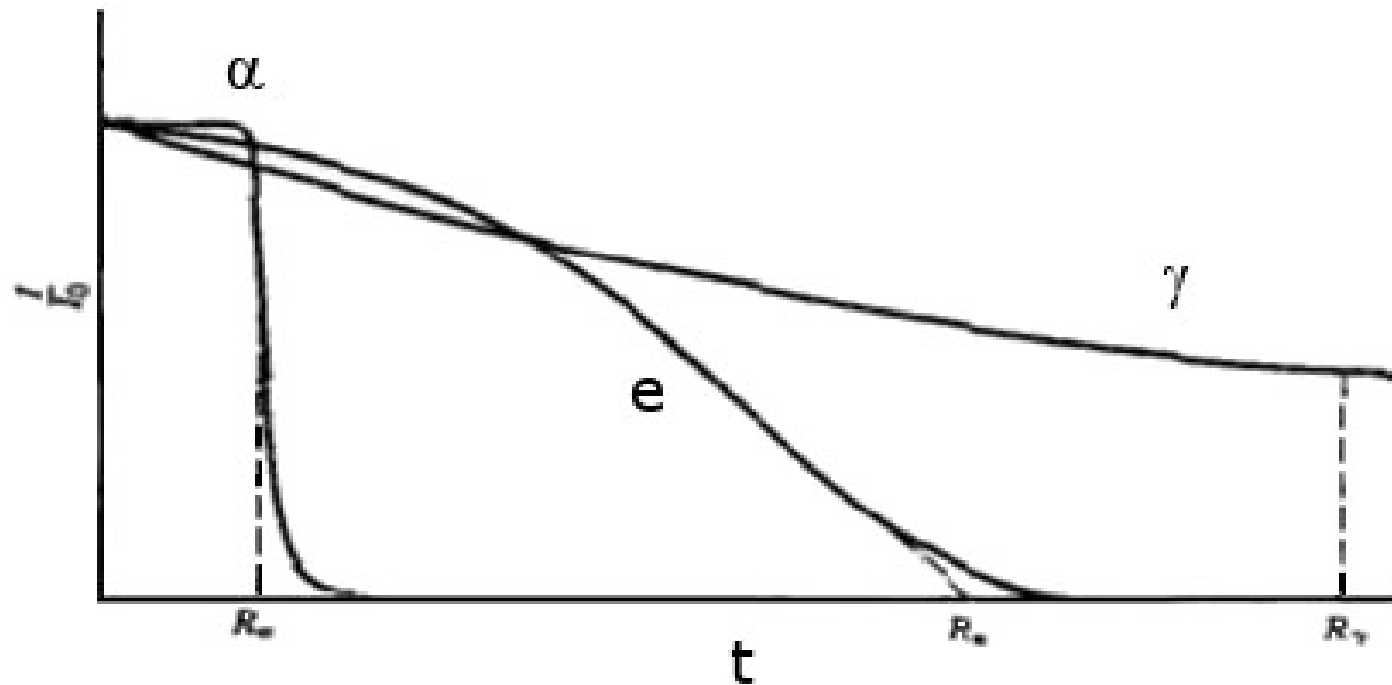
## “rivelatore medio”

$$h\nu < 2m_e c^2$$

$$h\nu \gg 2m_e c^2$$



## Interazione di particelle cariche e radiazione e.m. con la materia



**Figure 7.11** The transmitted intensity measured in a geometry such as that shown in Figure 7.9. For  $\alpha$ 's, the value of  $t$  such that  $I/I_0 = 0.5$  is the mean range; for photons, with their simple exponential dependence, we can define the mean range similarly. For electrons, it is customary to define the *extrapolated range* by extending the linear portion of the absorption curve as shown. The horizontal scale is not at all linear; the range for  $\gamma$ 's may be  $10^4$  that for  $\alpha$ 's.